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function LIKELIHOOD-WEIGHTING( $X, \mathbf{e}, bn, N$ ) returns an estimate of  $\mathbf{P}(X|\mathbf{e})$ 
  inputs:  $X$ , the query variable
             $\mathbf{e}$ , observed values for variables  $\mathbf{E}$ 
             $bn$ , a Bayesian network specifying joint distribution  $\mathbf{P}(X_1, \dots, X_n)$ 
             $N$ , the total number of samples to be generated
  local variables:  $\mathbf{W}$ , a vector of weighted counts for each value of  $X$ , initially zero

  for  $j = 1$  to  $N$  do
     $\mathbf{x}, w \leftarrow$  WEIGHTED-SAMPLE( $bn, \mathbf{e}$ )
     $\mathbf{W}[x] \leftarrow \mathbf{W}[x] + w$  where  $x$  is the value of  $X$  in  $\mathbf{x}$ 
  return NORMALIZE( $\mathbf{W}$ )

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function WEIGHTED-SAMPLE( $bn, \mathbf{e}$ ) returns an event and a weight
   $w \leftarrow 1$ ;  $\mathbf{x} \leftarrow$  an event with  $n$  elements initialized from  $\mathbf{e}$ 
  foreach variable  $X_i$  in  $X_1, \dots, X_n$  do
    if  $X_i$  is an evidence variable with value  $x_i$  in  $\mathbf{e}$ 
      then  $w \leftarrow w \times P(X_i = x_i | \text{parents}(X_i))$ 
      else  $\mathbf{x}[i] \leftarrow$  a random sample from  $\mathbf{P}(X_i | \text{parents}(X_i))$ 
  return  $\mathbf{x}, w$ 

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**Figure 14.14** The likelihood-weighting algorithm for inference in Bayesian networks. In WEIGHTED-SAMPLE, each nonevidence variable is sampled according to the conditional distribution given the values already sampled for the variable's parents, while a weight is accumulated based on the likelihood for each evidence variable.

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function GIBBS-ASK( $X, \mathbf{e}, bn, N$ ) returns an estimate of  $\mathbf{P}(X|\mathbf{e})$ 
  local variables:  $\mathbf{N}$ , a vector of counts for each value of  $X$ , initially zero
                     $\mathbf{Z}$ , the nonevidence variables in  $bn$ 
                     $\mathbf{x}$ , the current state of the network, initially copied from  $\mathbf{e}$ 

  initialize  $\mathbf{x}$  with random values for the variables in  $\mathbf{Z}$ 
  for  $j = 1$  to  $N$  do
    for each  $Z_i$  in  $\mathbf{Z}$  do
      set the value of  $Z_i$  in  $\mathbf{x}$  by sampling from  $\mathbf{P}(Z_i | \text{mb}(Z_i))$ 
     $\mathbf{N}[x] \leftarrow \mathbf{N}[x] + 1$  where  $x$  is the value of  $X$  in  $\mathbf{x}$ 
  return NORMALIZE( $\mathbf{N}$ )

```

**Figure 14.15** The Gibbs sampling algorithm for approximate inference in Bayesian networks; this version cycles through the variables, but choosing variables at random also works.