COSC 545, Spring 2016: Problem Set #1

Due: Thur., 2/4, at the beginning of class (hand in hard copy).

Covers: Lectures 1 to 4.

Collaboration: You must work alone on the problem set and not consult outside sources. See the syllabus for details on the academic integrity policy for problem sets.

Problems

- 1. Provide formal arguments that regular languages are closed under intersection $(A \cap B = \{w \mid w \in A \land w \in B\})$ and complement $(\bar{A} = \{w \mid w \notin A\})$. Your arguments should use the same level of formal detail as the proof of closure under union presented in class and in the textbook.
- 2. For each of the following four languages, either prove it is non-regular (using the pumping lemma) or prove it regular (by drawing the state diagram of the finite automaton that accepts it):
 - (a) $\{w \mid w \in \{0,1\}^* \setminus \{0,1,00\}\}\$ (note: \ is the *set minus* operator).
 - (b) $\{w_1w_2w_1 \mid w_1, w_2 \in \{0, 1\}^*\}.$
 - (c) $\{a^ib^j \mid i,j>0, i \text{ and } j \text{ have different parities}\}$ (i.e., one is even and the other is odd).
 - (d) $\{w \# y \mid w, y \in \{a, b\}^*, w \neq y\}.$

(Note: The solution I have in mind for this final case is more involved than the solutions for the previous cases. You might find it useful to use what you proved in problem 1 about intersection and complement.)

- 3. Give a CFG generating the language of binary strings that are palindromes (i.e., read the same forward and backward).
- 4. Let a *neat PDA* be a variant of a PDA that only accepts a string if the machine ends in an accept state with an empty stack. Draw the state diagram for a *one state* neat PDA (your state diagram should only have one state) that accepts the language of strings from $\Sigma = \{a, b\}$ with an equal number of a and b's.