Empirical Methods in Natural Language Processing Lecture 9 N-gram Language Models

(most slides from Sharon Goldwater; some adapted from Alex Lascarides)

3 October 2016



Recap

- Thus far, we have talked mostly about *classification* given text as input.
- Today: we consider **sentence probabilities**: what are they, why are they useful, and how might we compute them?

Intuitive interpretation

- "Probability of a sentence" = how likely is it to occur in natural language
 - Consider only a specific language (English)

```
P(the cat slept peacefully) > P(slept the peacefully cat)
```

P(she studies morphosyntax) > P(she studies more faux syntax)

Language models in NLP

- It's very difficult to know the true probability of an arbitrary sequence of words.
- But we can define a language model that will give us good approximations.
- Like all models, language models will be good at capturing some things and less good for others.
 - We might want different models for different tasks.
 - Today, one type of language model: an N-gram model.

Spelling correction

Sentence probabilities help decide correct spelling.

mis-spelled text

the possible outputs

possible outputs

the possible output the po

Automatic speech recognition

Sentence probabilities help decide between similar-sounding options. speech input

↓ (Acoustic model)

possible outputs

She studies morphosyntax
She studies more faux syntax
She's studies morph or syntax

• • •

(Language model)

best-guess output

She studies morphosyntax

Machine translation

Sentence probabilities help decide word choice and word order.

onn-English input

↓ (Translation model)

possible outputs

She is going home
She is going house
She is traveling to home
To home she is going
...

↓ (Language model)

She is going home

LMs for prediction

- LMs can be used for **prediction** as well as correction.
- Ex: predictive text correction/completion on your mobile phone.
 - Keyboard is tiny, easy to touch a spot slightly off from the letter you meant.
 - Want to correct such errors as you go, and also provide possible completions.
 Predict as as you are typing: ineff...
- In this case, LM may be defined over sequences of *characters* instead of (or in addition to) sequences of words.

But how to estimate these probabilities?

- We want to know the probability of word sequence $\vec{w} = w_1 \dots w_n$ occurring in English.
- Assume we have some training data: large corpus of general English text.
- We can use this data to **estimate** the probability of \vec{w} (even if we never see it in the corpus!)

Probability theory vs estimation

- Probability theory can solve problems like:
 - I have a jar with 6 blue marbles and 4 red ones.
 - If I choose a marble uniformly at random, what's the probability it's red?

Probability theory vs estimation

- Probability theory can solve problems like:
 - I have a jar with 6 blue marbles and 4 red ones.
 - If I choose a marble uniformly at random, what's the probability it's red?
- But often we don't know the true probabilities, only have data:
 - I have a jar of marbles.
 - I repeatedly choose a marble uniformly at random and then replace it before choosing again.
 - In ten draws, I get 6 blue marbles and 4 red ones.
 - On the next draw, what's the probability I get a red marble?
- The latter also requires estimation theory.

Notation

- I will often omit the random variable in writing probabilities, using P(x) to mean P(X=x).
- When the distinction is important, I will use
 - -P(x) for *true* probabilities
 - $-\hat{P}(x)$ for estimated probabilities
 - $P_{\rm E}(x)$ for estimated probabilities using a particular estimation method E.
- But since we almost always mean estimated probabilities, may get lazy later and use P(x) for those too.

Example estimation: M&M colors

What is the proportion of each color of M&M?

• In 48 packages, I find¹ 2620 M&Ms, as follows:

Red	Orange	Yellow	Green	Blue	Brown
372	544	369	483	481	371

How to estimate probability of each color from this data?

 $^{^{1}}$ Actually, data from: https://joshmadison.com/2007/12/02/mms-color-distribution-analysis/

Relative frequency estimation

• Intuitive way to estimate discrete probabilities:

$$P_{\rm RF}(x) = \frac{C(x)}{N}$$

where C(x) is the count of x in a large dataset, and $N = \sum_{x'} C(x')$ is the total number of items in the dataset.

Relative frequency estimation

• Intuitive way to estimate discrete probabilities:

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- M&M example: $P_{RF}(red) = \frac{372}{2620} = .142$
- This method is also known as **maximum-likelihood estimation** (MLE) for reasons we'll get back to.

MLE for sentences?

Can we use MLE to estimate the probability of \vec{w} as a sentence of English? That is, the probability some sentence S has words \vec{w} ?

$$P_{\text{MLE}}(S = \vec{w}) = \frac{C(\vec{w})}{N}$$

where $C(\vec{w})$ is the count of \vec{w} in a large dataset, and N is the total number of sentences in the dataset.

Sentences that have never occurred

the Archaeopteryx soared jaggedly amidst foliage
vs
jaggedly trees the on flew

- Neither ever occurred in a corpus (until I wrote these slides). $\Rightarrow C(\vec{w}) = 0$ in both cases: MLE assigns both zero probability.
- But one is grammatical (and meaningful), the other not.
 ⇒ Using MLE on full sentences doesn't work well for language model estimation.

The problem with MLE

- MLE thinks anything that hasn't occurred will never occur (P=0).
- Clearly not true! Such things can have differering, and non-zero, probabilities:
 - My hair turns blue
 - I injure myself in a skiing accident
 - I travel to Finland
- And similarly for word sequences that have never occurred.

Sparse data

• In fact, even things that occur once or twice in our training data are a problem. Remember these words from Europarl?

cornflakes, mathematicians, pseudo-rapporteur, lobby-ridden, Lycketoft, UNCITRAL, policyfor, Commissioneris, 145.95

All occurred once. Is it safe to assume all have equal probability?

- This is a **sparse data** problem: not enough observations to estimate probabilities well. (Unlike the M&Ms, where we had large counts for all colours!)
- For sentences, many (most!) will occur rarely if ever in our training data. So we need to do something smarter.

Towards better LM probabilities

- One way to try to fix the problem: estimate $P(\vec{w})$ by combining the probabilities of smaller parts of the sentence, which will occur more frequently.
- This is the intuition behind **N-gram language models**.

- We want to estimate $P(S = w_1 \dots w_n)$.
 - Ex: P(S = the cat slept quietly).
- This is really a joint probability over the words in S: $P(W_1 = \text{the}, W_2 = \text{cat}, W_3 = \text{slept}, \dots W_4 = \text{quietly}).$
- Concisely, P(the, cat, slept, quietly) or $P(w_1, \dots w_n)$.

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- Concisely, P(the, cat, slept, quietly) or $P(w_1, \dots w_n)$.
- ullet Recall that for a joint probability, P(X,Y)=P(Y|X)P(X). So,

```
P(\text{the, cat, slept}) = P(\text{quietly}|\text{the, cat, slept})P(\text{the, cat, slept})
```

- = P(quietly|the, cat, slept)P(slept|the, cat)P(the, cat)
- = P(quietly|the, cat, slept)P(slept|the, cat)P(cat|the)P(the)

More generally, the chain rule gives us:

$$P(w_1, \dots w_n) = \prod_{i=1}^n P(w_i|w_1, w_2, \dots w_{i-1})$$

- But many of these conditional probs are just as sparse!
 - If we want P(I spent three years before the mast)...
 - we still need P(mast|I spent three years before the).

Example due to Alex Lascarides/Henry Thompson

- So we make an **independence assumption**: the probability of a word only depends on a fixed number of previous words (**history**).
 - trigram model: $P(w_i|w_1, w_2, \dots w_{i-1}) \approx P(w_i|w_{i-2}, w_{i-1})$
 - bigram model: $P(w_i|w_1, w_2, ..., w_{i-1}) \approx P(w_i|w_{i-1})$
 - unigram model: $P(w_i|w_1, w_2, \dots w_{i-1}) \approx P(w_i)$
- In our example, a trigram model says
 - $P(\text{mast}|\text{I spent three years before the}) \approx P(\text{mast}|\text{before the})$

Trigram independence assumption

- Put another way, trigram model assumes these are all equal:
 - P(mast|I spent three years before the)
 - P(mast|I went home before the)
 - P(mast|I saw the sail before the)
 - P(mast|I revised all week before the)

because all are estimated as P(mast|before the)

Also called a Markov assumption



Andrey Markov \rightarrow

Not always a good assumption! But it does reduce the sparse data problem.

Estimating trigram conditional probs

- We still need to estimate P(mast|before, the): the probability of mast given the two-word history before, the.
- If we use relative frequencies (MLE), we consider:
 - Out of all cases where we saw before, the as the first two words of a trigram,
 - how many had mast as the third word?

Estimating trigram conditional probs

• So, in our example, we'd estimate

$$P_{MLE}(\text{mast}|\text{before, the}) = \frac{C(\text{before, the, mast})}{C(\text{before, the})}$$

where C(x) is the count of x in our training data.

More generally, for any trigram we have

$$P_{MLE}(w_i|w_{i-2},w_{i-1}) = \frac{C(w_{i-2},w_{i-1},w_i)}{C(w_{i-2},w_{i-1})}$$

Example from Moby Dick corpus

$$C(\mathit{before}, \mathit{the}) = 55$$
 $C(\mathit{before}, \mathit{the}, \mathit{mast}) = 4$

$$\frac{C(\textit{before}, \textit{the}, \textit{mast})}{C(\textit{before}, \textit{the})} = 0.0727$$

- mast is the second most common word to come after before the in Moby Dick; wind is the most frequent word.
- $P_{MLE}(mast)$ is 0.00049, and $P_{MLE}(mast|the)$ is 0.0029.
- So seeing before the vastly increases the probability of seeing mast next.

Trigram model: summary

• To estimate $P(\vec{w})$, use chain rule and make an indep. assumption:

$$P(w_1, \dots w_n) = \prod_{i=1}^n P(w_i|w_1, w_2, \dots w_{i-1})$$

$$\approx P(w_1)P(w_2|w_1) \prod_{i=3}^n P(w_i|w_{i-2}, w_{w-1})$$

Then estimate each trigram prob from data (here, using MLE):

$$P_{MLE}(w_i|w_{i-2},w_{i-1}) = \frac{C(w_{i-2},w_{i-1},w_i)}{C(w_{i-2},w_{i-1})}$$

 \bullet On your own: work out the equations for other N-grams (e.g., bigram, unigram).

Practical details (1)

• Trigram model assumes two word history:

$$P(\vec{w}) = P(w_1)P(w_2|w_1)\prod_{i=3}^{n} P(w_i|w_{i-2}, w_{w-1})$$

• But consider these sentences:

$$w_1$$
 w_2 w_3 w_4
(1) he saw the yellow
(2) feeds the cats daily

What's wrong? Does the model capture these problems?

Beginning/end of sequence

 To capture behaviour at beginning/end of sequences, we can augment the input:

$$w_{-1}$$
 w_0 w_1 w_2 w_3 w_4 w_5
(1) $<$ s> $<$ s> he saw the yellow $<$ /s>
(2) $<$ s> $<$ s> feeds the cats daily $<$ /s>

• That is, assume $w_{-1}=w_0=$ <s> and $w_{n+1}=$ </s> so:

$$P(\vec{w}) = \prod_{i=1}^{n+1} P(w_i|w_{i-2}, w_{i-1})$$

• Now, P(</s>|the, yellow) is low, indicating this is not a good sentence.

Beginning/end of sequence

 Alternatively, we could model all sentences as one (very long) sequence, including punctuation:

```
two cats live in sam 's barn . sam feeds the cats daily . yesterday , he saw the yellow cat catch a mouse . [...]
```

- ullet Now, trigrams like $P(.|{\tt cats\ daily})$ and $P(,|.\ {\tt yesterday})$ tell us about behavior at sentence edges.
- Here, all tokens are lowercased. What are the pros/cons of not doing that?

Practical details (2)

- Word probabilities are typically very small.
- Multiplying lots of small probabilities quickly gets so tiny we can't represent the numbers accurately, even with double precision floating point.
- So in practice, we typically use negative log probabilities (sometimes called costs):
 - Since probabilities range from 0 to 1, negative log probs range from 0 to ∞ : lower cost = higher probability.
 - Instead of *multiplying* probabilities, we *add* neg log probabilities.

Interim Summary: N-gram probabilities

- "Probability of a sentence": how likely is it to occur in natural language? Useful in many natural language applications.
- We can never know the true probability, but we may be able to estimate it from corpus data.
- N-gram models are one way to do this:
 - To alleviate sparse data, assume word probs depend only on short history.
 - Tradeoff: longer histories may capture more, but are also more sparse.
 - So far, we estimated N-gram probabilites using MLE.

Interim Summary: Language models

• Language models tell us $P(\vec{w}) = P(w_1 \dots w_n)$: How likely to occur is this sequence of words?

Roughly: Is this sequence of words a "good" one in my language?

- LMs are used as a component in applications such as speech recognition, machine translation, and predictive text completion.
- To reduce sparse data, N-gram LMs assume words depend only on a fixed-length history, even though we know this isn't true.

Coming up next:

- Weaknesses of MLE and ways to address them (more issues with sparse data).
- How to evaluate a language model: are we estimating sentence probabilities accurately?

Evaluating a language model

- Intuitively, a trigram model captures more context than a bigram model, so should be a "better" model.
- That is, it should more accurately predict the probabilities of sentences.
- But how can we measure this?

Two types of evaluation in NLP

- Extrinsic: measure performance on a downstream application.
 - For LM, plug it into a machine translation/ASR/etc system.
 - The most reliable evaluation, but can be time-consuming.
 - And of course, we still need an evaluation measure for the downstream system!
- Intrinsic: design a measure that is inherent to the current task.
 - Can be much quicker/easier during development cycle.
 - But not always easy to figure out what the right measure is: ideally, one that correlates well with extrinsic measures.

Let's consider how to define an intrinsic measure for LMs.

Entropy

• Definition of the **entropy** of a random variable X:

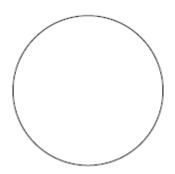
$$H(X) = \sum_{x} -P(x) \log_2 P(x)$$

- Intuitively: a measure of uncertainty/disorder
- Also: the expected value of $-\log_2 P(X)$

One event (outcome)

$$P(a) = 1$$

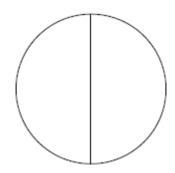
$$H(X) = -1\log_2 1$$
$$= 0$$



2 equally likely events:

$$P(a) = 0.5$$
$$P(b) = 0.5$$

$$H(X) = -0.5 \log_2 0.5 - 0.5 \log_2 0.5$$
$$= -\log_2 0.5$$
$$= 1$$

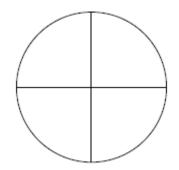


4 equally likely events:

$$P(a) = 0.25$$

 $P(b) = 0.25$
 $P(c) = 0.25$
 $P(d) = 0.25$

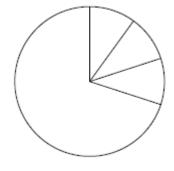
$$H(X) = -0.25 \log_2 0.25 - 0.25 \log_2 0.25$$
$$-0.25 \log_2 0.25 - 0.25 \log_2 0.25$$
$$= -\log_2 0.25$$
$$= 2$$



3 equally likely events and one more a = 0.7

$$P(a) = 0.7$$

 $P(b) = 0.1$
 $P(c) = 0.1$
 $P(d) = 0.1$



$$H(X) = -0.7 \log_2 0.7 - 0.1 \log_2 0.1$$

$$-0.1 \log_2 0.1 - 0.1 \log_2 0.1$$

$$= -0.7 \log_2 0.7 - 0.3 \log_2 0.1$$

$$= -(0.7)(-0.5146) - (0.3)(-3.3219)$$

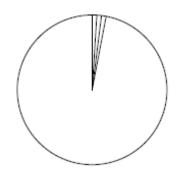
$$= 0.36020 + 0.99658$$

$$= 1.35678$$

3 equally likely events and one much more likely than the others:

$$P(a) = 0.97$$

 $P(b) = 0.01$
 $P(c) = 0.01$
 $P(d) = 0.01$



$$H(X) = -0.97 \log_2 0.97 - 0.01 \log_2 0.01$$

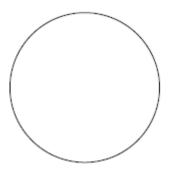
$$-0.01 \log_2 0.01 - 0.01 \log_2 0.01$$

$$= -0.97 \log_2 0.97 - 0.03 \log_2 0.01$$

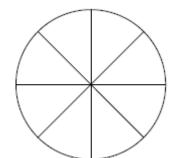
$$= -(0.97)(-0.04394) - (0.03)(-6.6439)$$

$$= 0.04262 + 0.19932$$

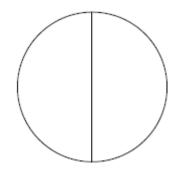
$$= 0.24194$$



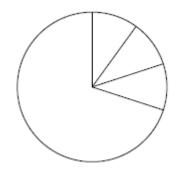
$$H(X) = 0$$



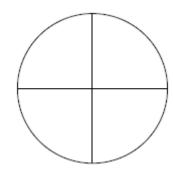
$$H(X) = 3$$



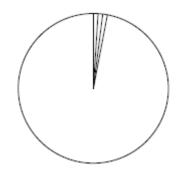
H(X) = 1



H(X) = 1.35678



H(X) = 2



H(X) = 0.24194

Entropy as y/n questions

How many yes-no questions (bits) do we need to find out the outcome?

- Uniform distribution with 2^n outcomes: n q's.
- Other cases: entropy is the average number of questions per outcome in a (very) long sequence of outcomes, where questions can consider multiple outcomes at once.

Entropy as encoding sequences

- ullet Assume that we want to encode a sequence of events X.
- Each event is encoded by a sequence of bits, we want to use as few bits as possible.
- For example
 - Coin flip: heads = 0, tails = 1
 - 4 equally likely events: a=00, b=01, c=10, d=11
 - 3 events, one more likely than others: a = 0, b = 10, c = 11
 - Morse code: e has shorter code than q
- ullet Average number of bits needed to encode $X \geq$ entropy of X

The Entropy of English

- Given the start of a text, can we guess the next word?
- For humans, the measured entropy is only about 1.3.
 - Meaning: on average, given the preceding context, a human would need only 1.3 y/n questions to determine the next word.
 - This is an upper bound on the true entropy, which we can never know (because we don't know the true probability distribution).
- But what about N-gram models?

Cross-entropy

- Our LM estimates the probability of word sequences.
- A good model assigns high probability to sequences that actually have high probability (and low probability to others).
- Put another way, our model should have low uncertainty (entropy) about which word comes next.
- We can measure this using cross-entropy.
- Note that cross-entropy \geq entropy: our model's uncertainty can be no less than the true uncertainty.

Computing cross-entropy

• For $w_1 \dots w_n$ with large n, per-word cross-entropy is well approximated by:

$$H_M(w_1 \dots w_n) = -\frac{1}{n} \log_2 P_M(w_1 \dots w_n)$$

- This is just the average negative log prob our model assigns to each word in the sequence. (i.e., normalized for sequence length).
- Lower cross-entropy ⇒ model is better at predicting next word.

Cross-entropy example

Using a bigram model from Moby Dick, compute per-word cross-entropy of I spent three years before the mast (here, without using end-of sentence padding):

```
\begin{array}{ll} -\frac{1}{7}(& \lg_2(P(\mathit{I})) + \lg_2(P(\mathit{spent}|\mathit{I})) + \lg_2(P(\mathit{three}|\mathit{spent})) + \lg_2(P(\mathit{years}|\mathit{three})) \\ & + \lg_2(P(\mathit{before}|\mathit{years})) + \lg_2(P(\mathit{the}|\mathit{before})) + \lg_2(P(\mathit{mast}|\mathit{the})) \\ = & -\frac{1}{7}(& -6.9381 - 11.0546 - 3.1699 - 4.2362 - 5.0 - 2.4426 - 8.4246 \\ = & -\frac{1}{7}(& 41.2660 & ) \\ \approx & 6 \end{array}
```

- Per-word cross-entropy of the *unigram* model is about 11.
- So, unigram model has about 5 bits more uncertainty per word then bigram model. But, what does that mean?

Data compression

- If we designed an optimal code based on our bigram model, we could encode the entire sentence in about 42 bits.
- A code based on our unigram model would require about 77 bits.
- ASCII uses an average of 24 bits per word (168 bits total)!
- So better language models can also give us better data compression: as elaborated by the field of **information theory**.

Perplexity

- LM performance is often reported as **perplexity** rather than cross-entropy.
- Perplexity is simply 2^{cross-entropy}
- The average branching factor at each decision point, if our distribution were uniform.
- So, 6 bits cross-entropy means our model perplexity is $2^6 = 64$: equivalent uncertainty to a uniform distribution over 64 outcomes.

Interpreting these measures

I measure the cross-entropy of my LM on some corpus as 5.2. Is that good?

Interpreting these measures

I measure the cross-entropy of my LM on some corpus as 5.2. Is that good?

- No way to tell! Cross-entropy depends on both the model and the corpus.
 - Some language is simply more predictable (e.g. casual speech vs academic writing).
 - So lower cross-entropy could mean the corpus is "easy", or the model is good.
- We can only compare different models on the same corpus.
- Should we measure on training data or held-out data? Why?

Sparse data, again

Suppose now we build a *trigram* model from Moby Dick and evaluate the same sentence.

- But I spent three never occurs, so $P_{MLE}(\text{three} \mid \text{I spent}) = 0$
- which means the cross-entropy is infinite.
- Basically right: our model says I spent three should never occur, so our model is infinitely wrong/surprised when it does!
- ullet Even with a unigram model, we will run into words we never saw before. So even with short N-grams, we need better ways to estimate probabilities from sparse data.

Smoothing

- The flaw of MLE: it estimates probabilities that make the training data maximally probable, by making everything else (unseen data) minimally probable.
- **Smoothing** methods address the problem by stealing probability mass from seen events and reallocating it to unseen events.
- Lots of different methods, based on different kinds of assumptions. We will discuss just a few.

Add-One (Laplace) Smoothing

• Just pretend we saw everything one more time than we did.

$$P_{\mathrm{ML}}(w_i|w_{i-2},w_{i-1}) = \frac{C(w_{i-2},w_{i-1},w_i)}{C(w_{i-2},w_{i-1})}$$

$$\Rightarrow P_{+1}(w_i|w_{i-2},w_{i-1}) = \frac{C(w_{i-2},w_{i-1},w_i)+1}{C(w_{i-2},w_{i-1})}$$

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• NO! Sum over possible w_i (in vocabulary V) must equal 1:

$$\sum_{w_i \in V} P(w_i | w_{i-2}, w_{i-1}) = 1$$

• If increasing the numerator, must change denominator too.

Add-one Smoothing: normalization

• We want:

$$\sum_{w_i \in V} \frac{C(w_{i-2}, w_{i-1}, w_i) + 1}{C(w_{i-2}, w_{i-1}) + x} = 1$$

• Solve for *x*:

$$\sum_{w_{i} \in V} (C(w_{i-2}, w_{i-1}, w_{i}) + 1) = C(w_{i-2}, w_{i-1}) + x$$

$$\sum_{w_{i} \in V} C(w_{i-2}, w_{i-1}, w_{i}) + \sum_{w_{i} \in V} 1 = C(w_{i-2}, w_{i-1}) + x$$

$$C(w_{i-2}, w_{i-1}) + v = C(w_{i-2}, w_{i-1}) + x$$

$$v = x$$

where v = vocabulary size.

Add-one example (1)

- Moby Dick has one trigram that begins I spent (it's I spent in) and the vocabulary size is 17231.
- Comparison of MLE vs Add-one probability estimates:

	MLE	+1
$\hat{P}(\text{three} \mid \text{I spent})$	0	0.00006
$\hat{P}(ext{in} \mid ext{I spent})$	1	0.0001

• $\hat{P}(\text{in}|\text{I spent})$ seems very low, especially since in is a very common word. But can we find better evidence that this method is flawed?

Add-one example (2)

• Suppose we have a more common bigram w_1, w_2 that occurs 100 times, 10 of which are followed by w_3 .

$$\begin{array}{c|cccc}
 & \text{MLE} & +1 \\
 & \hat{P}(w_3|w_1, w_2) & \frac{10}{100} & \frac{11}{17331} \\
 & \approx 0.0006
\end{array}$$

- Shows that the very large vocabulary size makes add-one smoothing steal way too much from seen events.
- In fact, MLE is pretty good for frequent events, so we shouldn't want to change these much.

Add- α (Lidstone) Smoothing

• We can improve things by adding $\alpha < 1$.

$$P_{+\alpha}(w_i|w_{i-1}) = \frac{C(w_{i-1}, w_i) + \alpha}{C(w_{i-1}) + \alpha v}$$

- Like Laplace, assumes we know the vocabulary size in advance.
- But if we don't, can just add a single "unknown" (UNK) item to the vocabulary, and use this for all unknown words during testing.
- Then: how to choose α ?

Optimizing α (and other model choices)

- Use a three-way data split: **training** set (80-90%), **held-out** (or **development**) set (5-10%), and **test** set (5-10%)
 - Train model (estimate probabilities) on training set with different values of α
 - Choose the α that minimizes cross-entropy on development set
 - Report final results on test set.
- More generally, use dev set for evaluating different models, debugging, and optimizing choices. Test set simulates deployment, use it only once!
- Avoids overfitting to the training set and even to the test set.

Summary

- We can measure the relative goodness of LMs on the same corpus using cross-entropy: how well does the model predict the next word?
- ullet We need smoothing to deal with unseen N-grams.
- Add-1 and Add- α are simple, but not very good.
- We'll see even better smoothing methods next time.