Elements of Algorithms

Mark Maloof Department of Computer Science Washington, DC 20057

September 22, 2016

Four Critical Elements

- Algorithms have some subset of the following critical elements:
 - 1. simple statements, including but not limited to:
 - input statements
 - assignment statements
 - output statements
 - return statements
 - 2. sequences of statements, which are also statements

- 3. branching statements
- 4. looping statements

Algorithm for Simple Interest

- 1: input r, b, and m
- 2: $i \leftarrow r \cdot b \cdot m$
- 3: output i

input statement
 assignment statement
 output statement

Another Algorithm for Simple Interest

- 1: input r
- 2: **input** *b*
- 3: **input** *m*
- 4: $i \leftarrow r$
- 5: $i \leftarrow i \cdot b$
- 6: $i \leftarrow i \cdot m$
- 7: output i

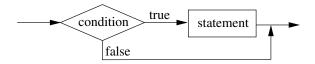
- ▷ input statement
- \triangleright input statement
- ▷ input statement
- > assignment statement
- > assignment statement
- > assignment statement
 - ▷ output statement

Branching: If-then Statement

if some condition is true then
 statement (or sequence)
end if

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

Flowchart for an if-then Statement



◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

Example of an if-then Statement

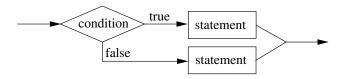
- 1: input grade
- 2: if grade > 64 then
- 3: output pass
- 4: end if
- 5: if grade ≤ 64 then

- 6: **output** fail
- 7: end if

Branching: If-then-else Statement

if some condition is true then
 statement (or sequence)
else
 statement (or sequence)
end if

Flowchart for an if-then-else Statement



◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

Example of an if-then-else Statement

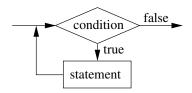
- 1: input grade
- 2: if grade > 64 then
- 3: output pass
- 4: **else**
- 5: **output** fail
- 6: **end if**

Looping: While Statement, While Loop

while some condition is true do
 statement (or sequence)
end while

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

Flowchart for a While Loop





Example of a While Loop

input grade
 while there is a grade do
 if grade > 64 then
 output pass
 else
 output fail
 end if
 input grade
 and while

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

9: end while

Repeat-until Loop

repeat statement (or sequence) until some condition is true

Equivalent to:

statement (or sequence)
while some condition is false do
 statement (or sequence)
end while

For Loop

for $i \leftarrow b, e$ do statement (or sequence) end for

Equivalent to:

 $i \leftarrow b$ while $i \le e$ do statement (or sequence) $i \leftarrow i + 1$ end while

For-each Loop

for each element of some collection do statement (or sequence) end for

Equivalent to:

 $i \leftarrow 1$ $e \leftarrow$ the number of elements in the collection while $i \le e$ do $element \leftarrow i$ th element of the collection statement (or sequence) $i \leftarrow i + 1$ end while

Example of a For-each Loop

1: Let Grades be a sequence or list of grades

- 2: input Grades
- 3: for each grade in Grades do
- 4: **if** grade > 64 **then**
- 5: output pass
- 6: **else**
- 7: **output** fail
- 8: end if
- 9: end for

Algorithm for Binary-to-Decimal Conversion

1: Let D be a decimal number, set to zero

- 2: Let B be a binary number, set to zero
- 3: **input** *B*
- 4: Let B' be B with its digits reversed
- 5: $i \leftarrow 0$
- 6: for each binary digit $b \in B'$ do
- 7: $D \leftarrow D + b \cdot 2^i$
- 8: $i \leftarrow i+1$
- 9: end for
- 10: output D

Program for B2D Conversion in Julia

```
D = 0
B = {1,1,0,0,1}
BPrime = B[end:-1:1]
i = 0
for b in BPrime
D = D + b * 2<sup>i</sup>
i = i + 1
end
println(D)
```

Program for B2D Conversion in C

```
#include <stdio.h>
#include <math.h>
int main()
ł
  int b[] = { 1, 0, 0, 1, 1 };
  int n = 5;
  int d = 0;
  int i = 0;
  for (i = n - 1; i \ge 0; i = i - 1) {
    d = d + b[i] * (int) pow(2.0, i);
  }
  printf( "%d\n", d );
  return 0;
}
```

▲ロト ▲帰 ト ▲ ヨ ト ▲ ヨ ト ・ ヨ ・ の Q ()

Algorithm for Decimal-to-Binary Conversion

1: Let B be an empty sequence of binary digits

- 2: Let D be a decimal number, set to zero
- 3: **input** *D*
- 4: while $D \neq 0$ do
- 5: $r \leftarrow D \mod 2$
- 6: Add r as the left-most digit of B
- 7: $D \leftarrow D \div 2$ (integer division)
- 8: end while
- 9: **output** *B*

Program for D2B Conversion in Julia

▲□▶ ▲圖▶ ▲臣▶ ▲臣▶ ―臣 … のへで

```
B = {}
D = 25
while D > 0
    r = D % 2
    unshift!( B, r )
    D = div( D, 2 )
end
println( B )
```

Program for D2B Conversion in C

```
#include <stdio.h>
#include <math.h>
int main()
ſ
 int d = 25;
 int n = (int) ceil( log2( d ) );
 int b[n]:
 int i = n - 1;
 int r = 0;
 while (d > 0) {
   r = d \% 2;
   b[i] = r;
   i = i - 1;
   d = d / 2;
 }
 for ( i = 0; i < n; i = i + 1 ) {
   printf( "%d", b[i] );
 3
 printf( "\n" );
 return 0;
}
```

▲□▶ ▲□▶ ▲□▶ ▲□▶ □ のQ@