Linear Models for Classification: Features & Weights

Nathan Schneider (some slides borrowed from Chris Dyer) ENLP | 4 February 2019

Outline

Words, probabilities → Features, weights

this lecture

- Geometric view: decision boundary
- Perceptron next lecture
- Generative vs. Discriminative
- More discriminative models: Logistic regression/MaxEnt;
 SVM
- Loss functions, optimization
- Regularization; sparsity

Word Sense Disambiguation (WSD)

- Given a word in context, predict which sense is being used.
 - Evaluated on corpora such as SemCor, which is fully annotated for WordNet synsets.
- For example: consider joint POS & WSD classification for 'interest', with 3 senses:
 - N:financial (I repaid the loan with interest)
 - N:nonfinancial (I read the news with interest)
 - V:nonfinancial (Can I interest you in a dessert?)

Beyond BoW

- Neighboring words are relevant to this decision.
- More generally, we can define features of the input that may help identify the correct class.
 - Individual words
 - Bigrams (pairs of consecutive words: Wall Street)
 - Capitalization (interest vs. Interest vs. INTEREST)
 - Metadata: document genre, author, ...
- These can be used in naïve Bayes: "bag of features"
 - With overlapping features, independence assumption is even more naïve: p(y | x) ∝ p(y) ··· p(Wall | y) p(Street | y) p(Wall Street | y)

Choosing Features

- Supervision means that we don't have to pre-specify the precise relationship between each feature and the classification outcomes.
- But domain expertise helps in choosing which kinds of features to include in the model. (words, subword units, metadata, ...)
 - And sometimes, highly task-specific features are helpful.
- The decision about what features to include in a model is called feature engineering.
 - (There are some algorithmic techniques, such as *feature selection*, that can assist in this process.)
 - More features = more flexibility, but also more expensive to train, more opportunity for overfitting.

	b	(X	1
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	$\Psi(X)$
bias	1
capitalized?	0
#wordsBefore	6
#wordsAfter	3
relativeOffset	0.66
leftWord=about	1
leftWord=best	0
rightWord=rates	1
rightWord=in	0
Wall	1
Street	1
vets	1
best	0
in	0
Wall Street	1
Street vets	1
vets raise	1

x = Wall Street vets raise concerns about interest rates, politics

bias feature (≈class prior): value of 1 for every **x** so the learned weight will reflect prevalence of the class

- Turns the input into a table of features with real values (often binary: 0 or 1).
- In practice: define feature templates like "leftWord=•" from which specific features are instantiated

φ((\mathbf{x})
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spelling feature

- Turns the input into a table of features with real values (often binary: 0 or 1).
- In practice: define feature templates like "leftWord=•" from which specific features are instantiated

	$\phi(x)$
bias	1
pitalized?	0
ordoRoforo	6

capitalized? 0

#wordsBefore 6

#wordsAfter 3

relativeOffset 0.66

leftWord=about 1 leftWord=best 0

rightWord=rates 1

rightWord=in 0 Wall 1

Street 1 vets 1

best 0

in 0

Wall Street 1

Street vets 1 vets raise 1

x = Wall Street vets raise concerns about interest rates, politics

token positional features

- Turns the input into a table of features with real values (often binary: 0 or 1).
- In practice: define feature templates like "leftWord=•" from which specific features are instantiated

	$\phi(x)$
bias	1
capitalized?	0
#wordsBefore	6

#wordsAfter relativeOffset 0.66

leftWord=about leftWord=best rightWord=rates rightWord=in

Wall	1
Street	1
vets	1
best	0
in	0
Wall Street	1
Street vets	1
vets raise	1

x = Wall Street vets raise concernsabout interest rates, politics

immediately neighboring words

- Turns the input into a table of features with real values (often binary: 0 or 1).
- In practice: define feature templates like "leftWord=•" from which specific features are instantiated

	$\phi(x)$
bias	1
capitalized?	0
#wordsBefore	6
#wordsAfter	3
relativeOffset	0.66
leftWord=about	1
leftWord=best	0
rightWord=rates	1
rightWord=in	0
Wall	1
Street	1
vets	1
best	0
in	0
Wall Street	1
Street vets	1
vets raise	1

x = Wall Street vets raise concerns about interest rates, politics

unigrams

- Turns the input into a table of features with real values (often binary: 0 or 1).
- In practice: define feature templates like "leftWord=•" from which specific features are instantiated

	$\phi(x)$
bias	1
capitalized?	0
#wordsBefore	6
#wordsAfter	3
relativeOffset	0.66
leftWord=about	1
leftWord=best	0
rightWord=rates	1
rightWord=in	0
Wall	1
Street	1
vets	1
best	0
in	0
Wall Street	1
Street vets	1
vets raise	1

x = Wall Street vets raise concerns about interest rates, politics

- Turns the input into a table of features with real values (often binary: 0 or 1).
- In practice: define feature templates like "leftWord=•" from which specific features are instantiated

bigrams

	$\phi(x)$	$\phi(x')$
bias	1	1
capitalized?	0	0
#wordsBefore	6	3
#wordsAfter	3	8
relativeOffset	0.66	0.27
leftWord=about	1	0
leftWord=best	0	1
rightWord=rates	1	0
rightWord=in	0	1
Wall	1	0
Street	1	0
vets	1	1
best	0	1
in	0	1
Wall Street	1	0
Street vets	1	0
vets raise	1	0

- x = Wall Street vets raise concerns about interest rates, politics
- x' = Pet 's best interest in mind, but vets must follow law

- Turns the input into a table of features with real values (often binary: 0 or 1).
- In practice: define feature templates like "leftWord=•" from which specific features are instantiated

Linear Model

- For each input x (e.g., a document or word token), let $\phi(x)$ be a function that extracts a vector of its features.
 - Features may be binary (e.g., capitalized?) or real-valued (e.g., #word=debt).
- Each feature receives a real-valued **weight** parameter w. Each candidate label y' is scored for the token by summing the weights for the active features:

$$\mathbf{w}_{y'^{\mathsf{T}}}\mathbf{\phi}(\mathbf{x})$$

$$= \sum_{j} w_{y',j} \cdot \phi_{j}(\mathbf{x})$$

• For binary classification, equivalent to: $sign(\mathbf{w}^{\mathsf{T}} \mathbf{\phi}(\mathbf{x})) = +1$ or -1

	$\phi(x)$	W	$\phi(x')$
bias	1	-3.00	1
capitalized?	0	.22	0
#wordsBefore	6	01	3
#wordsAfter	3	.01	8
relativeOffset	0.6	1.00	0.2
leftWord=about	1	.00	0
leftWord=best	0	-2.00	1
rightWord=rates	1	5.00	0
rightWord=in	0	-1.00	1
Wall	1	1.00	0
Street	1	-1.00	0
vets	1	05	1
best	0	-1.00	1
in	0	01	1
Wall Street	1	4.00	0
Street vets	1	.00	0
vets raise	1	.00	0

- x = Wall Street vets raise concerns about interest rates, politics
- x' = Pet 's best interest in mind , but vets must follow law
 - Weights are learned from data
 - For the moment, assume binary classification: financial or nonfinancial
 - More positive weights more indicative of financial.
 - $\mathbf{w}^{\mathsf{T}} \mathbf{\phi}(\mathbf{x}) = 6.59$, $\mathbf{w}^{\mathsf{T}} \mathbf{\phi}(\mathbf{x}') = -6.74$

More then 2 classes

- Simply keep a separate weight vector for each class: \mathbf{w}_y
- The class whose weight vector gives the highest score wins!

Learning the weights

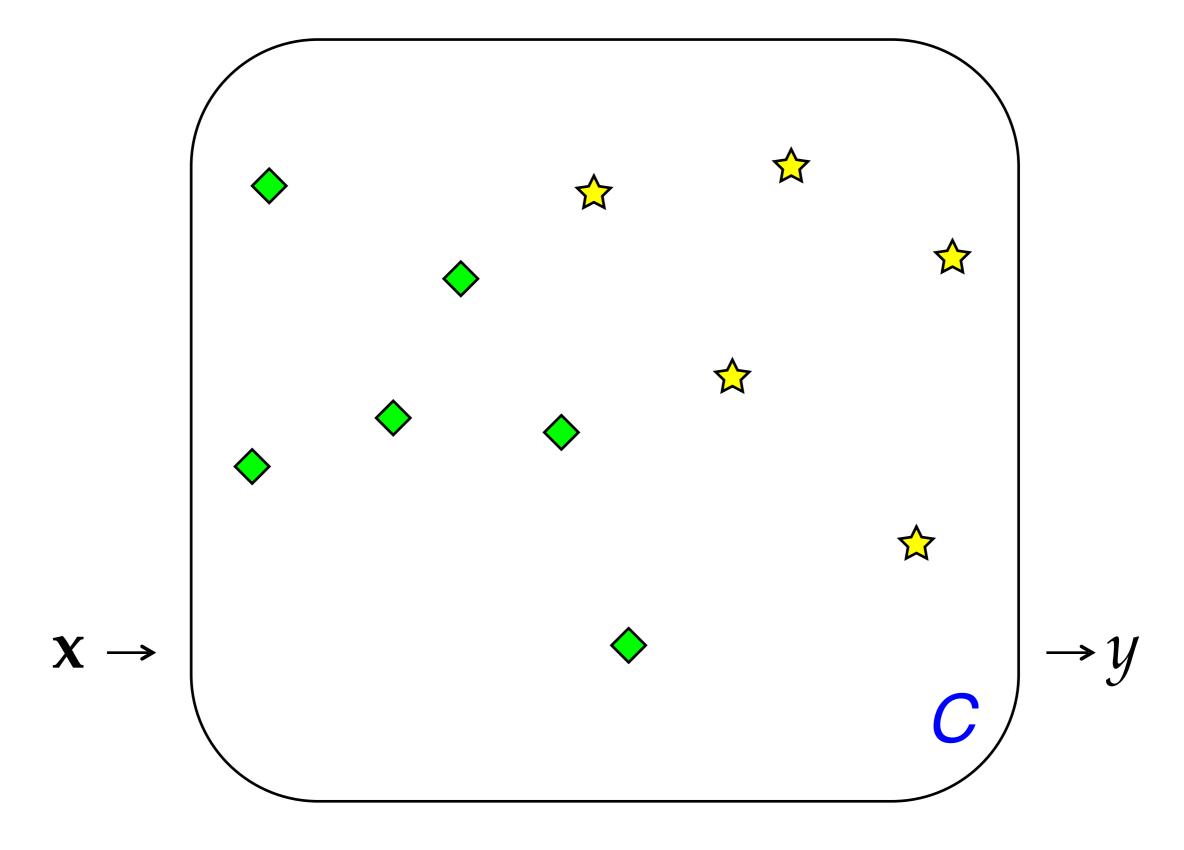
- Weights depend on the choice of model and learning algorithm.
- Naïve Bayes fits into this framework, under the following estimation procedure for w:
 - $w_{\text{bias}} = \log p(y)$
 - \forall features f: $w_f = \log p(f \mid y)$

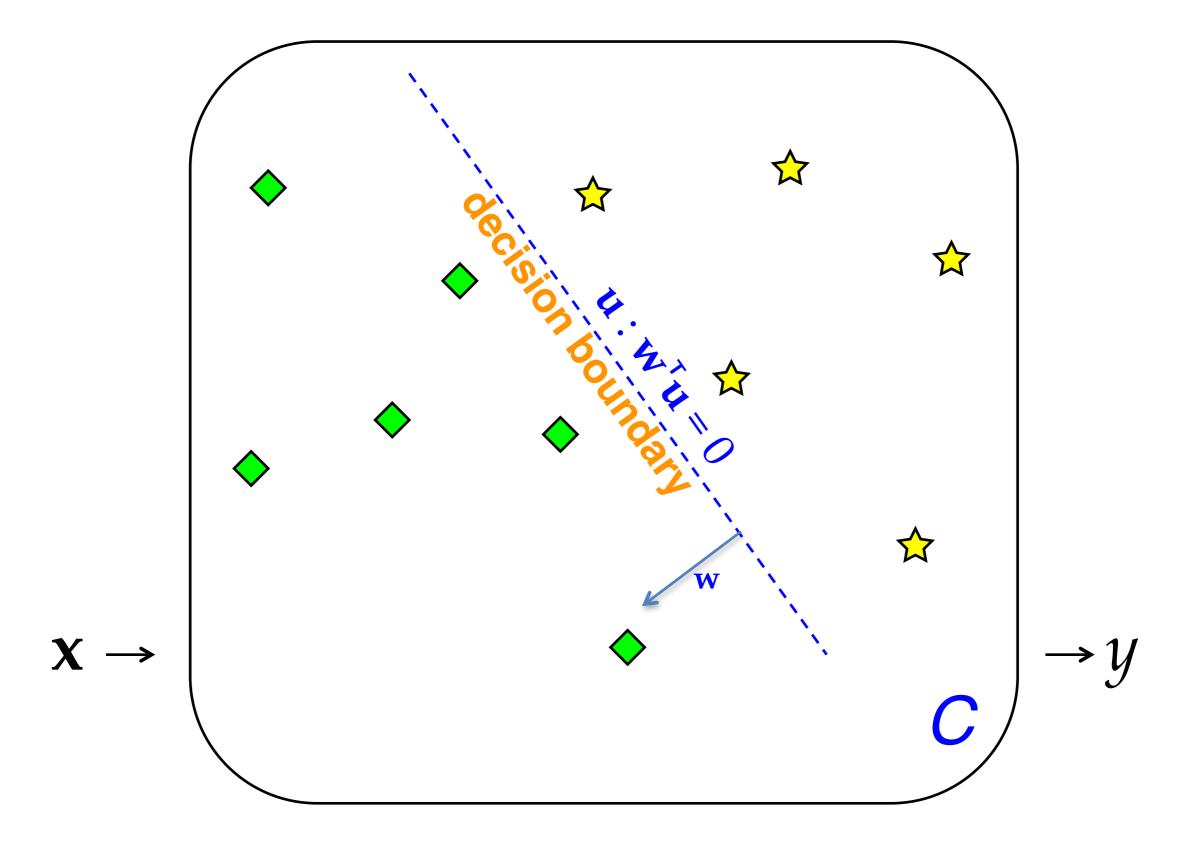
$$\Sigma_{j} w_{j} \cdot \phi_{j}(\mathbf{x}) = w_{\text{bias}} + \Sigma_{f \in \phi(\mathbf{x})} w_{f}$$

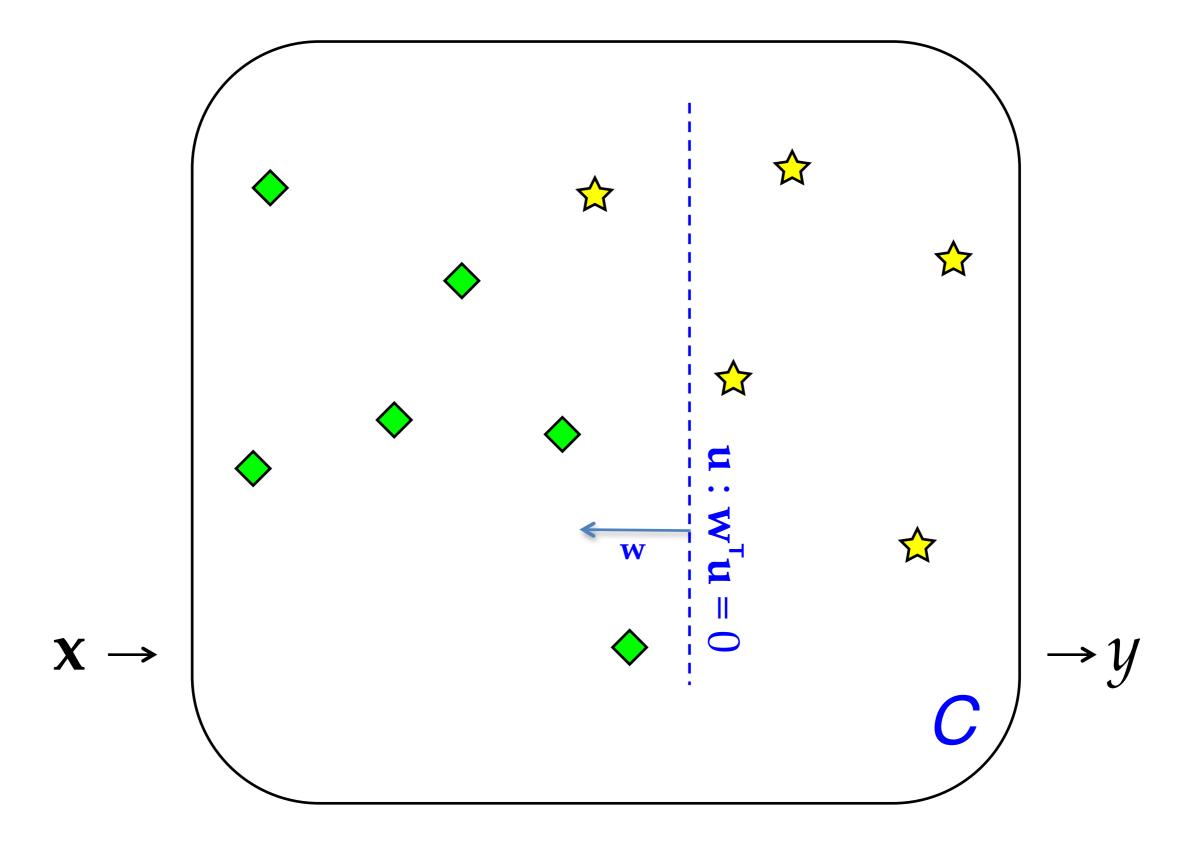
$$= \log p(y) + \Sigma_{f \in \phi(\mathbf{x})} \log p(f \mid y)$$

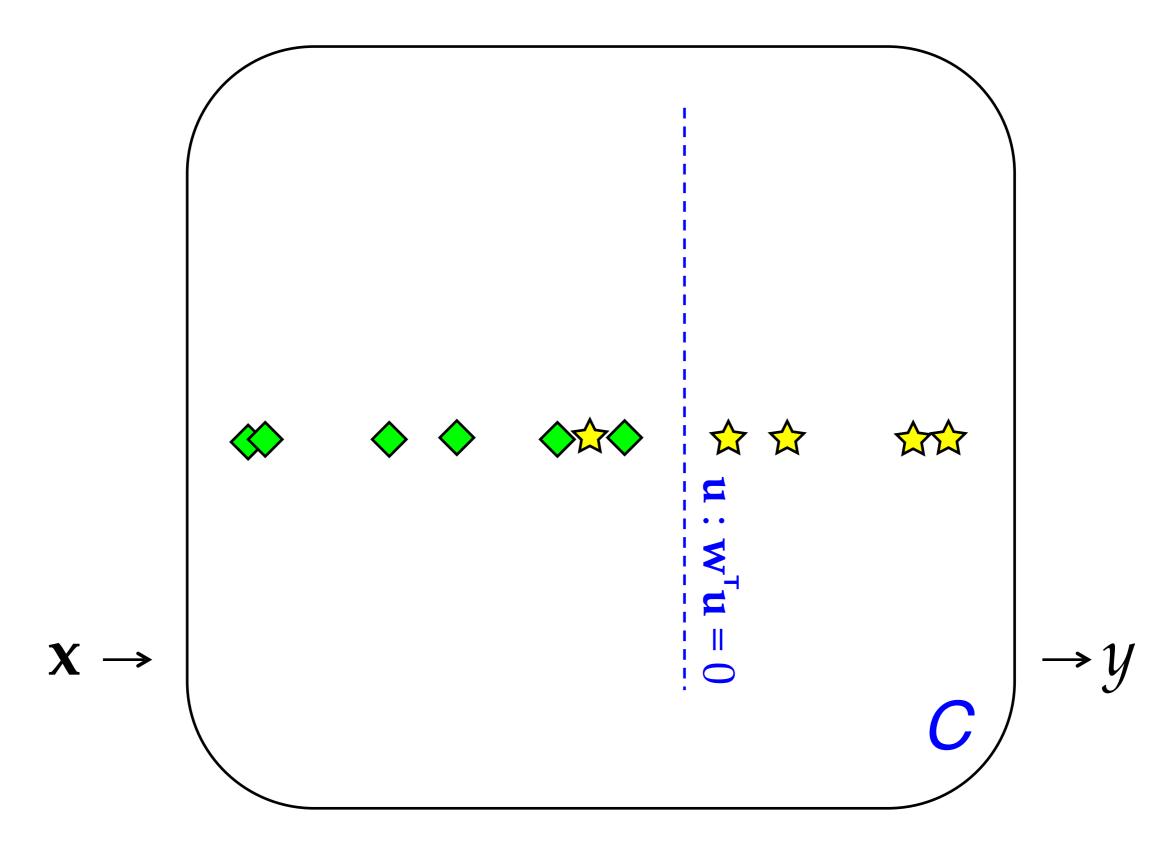
$$= \log (p(y) \cdot \Pi_{f \in \phi(\mathbf{x})} p(f \mid y))$$

- However, the naïve independence assumption—that all features are conditionally independent given the class—can be harmful.
 - Could the weights shown on the previous slide be naïve Bayes estimates?
 - * No, because some are positive (thus not log-probabilities). Other kinds of learning procedures can give arbitrary real-valued weights.
 - * If using log probabilities as weights, then the classification threshold should be equivalent to probability of .5, i.e. **log .5**.

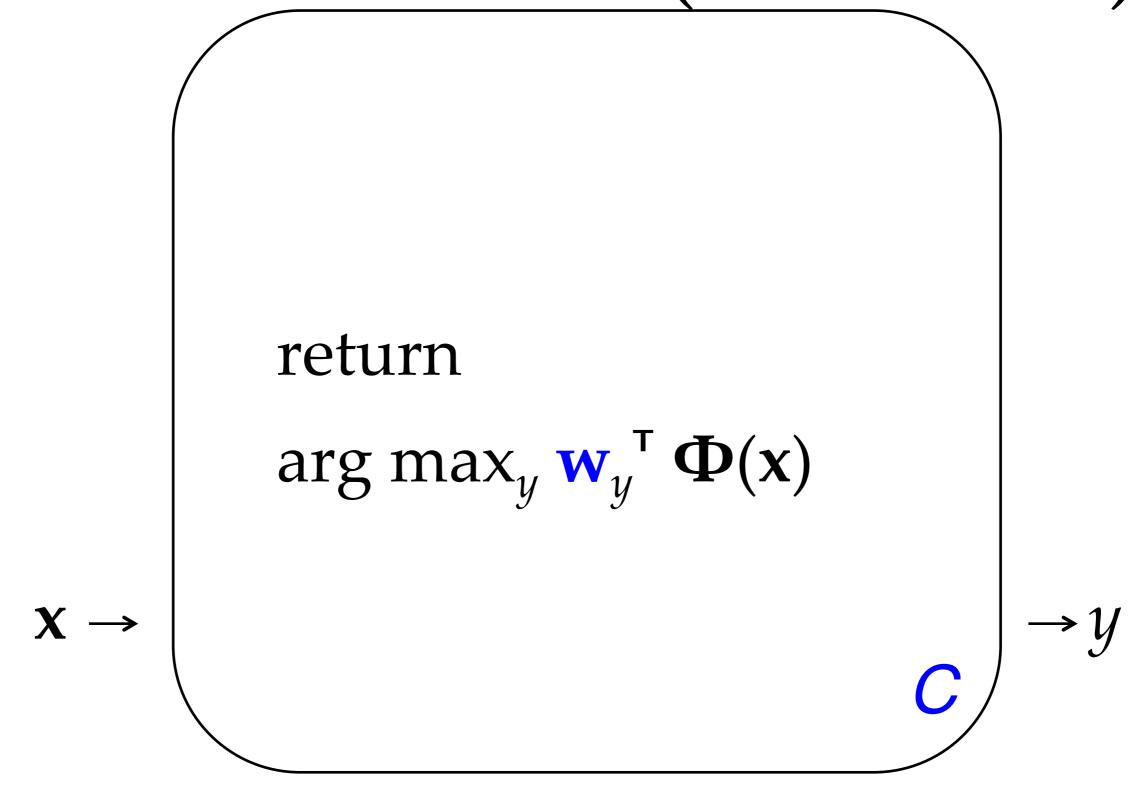








Linear Classifiers (> 2 Classes)



The term "feature"

- The term "feature" is overloaded in NLP/ML. Here are three different concepts:
 - Linguistic feature: in some formalisms, a symbolic property that applies to a unit to categorize it, e.g. [-voice] for a sound in phonology or [+past] for a verb in morphology.
 - Percept (or input feature): captures some aspect of an input x; binary- or real-valued. [The term "percept" is nonstandard but I think it is useful!]
 - Parameter (or model feature): an association between some percept and an output class (or structure) y for which a real-valued weight or score is learned. ends in $-ing \land y = VERB$